Network based early warning indicators of vegetation changes in a land-atmosphere model

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Abstract. Recent studies suggest that complex network based indicators may provide useful early warning signals of critical transitions in complex dynamic systems. In this study, such indicators are tested in a land-atmosphere coupled ecological model in which a scale-dependent infiltration feedback and a large-scale vegetation-precipitation feedback are represented. Multiple equilibria exist in this model and abrupt transitions can occur when precipitation is decreased. Interaction network based indicators of these transitions are compared with classical indicators of critical slowing down, such as the lag-1 autocorrelation, with particular focus on the transition associated with desertification. Three criteria are used to evaluate the quality of these early warning indicators and several high quality network based ones are identified.
1 Introduction

Ecosystems do not necessarily shift gradually with changes in the amount of resources (Scheffer et al., 2001; Claussen et al., 2013; Dekker, 2013). Observed patterns strongly suggest that multiple equilibria exist under similar climate regimes (Hirota et al., 2011; Staver et al., 2011b; Scheffer et al., 2012), which implies that ecosystems may shift from one equilibrium to another (Rietkerk et al., 2004; Hirota et al., 2011). Such abrupt transitions may lead to catastrophic changes of the landscape (Staver et al., 2011a) and in vegetation patterns (Rietkerk et al., 2004), which in turn strongly affects local climate through biophysical and biochemical feedbacks (Bonan, 2008; Seneviratne et al., 2010).

To anticipate potential catastrophic transition of ecosystems, numerous studies have tried to find early warning indicators of the transition to desertification (Rietkerk et al., 2004; kéfi et al., 2007; Scheffer et al., 2009; dakos et al., 2008). The phenomenon of ‘critical slowing down’, expressing that the recovery rate of the system to perturbations decreases near such a transition, has lead to useful early warning indicators, such as the lag-1 autocorrelation (Scheffer et al., 2009). Also indicators based on the changes in spatial correlation of vegetation patterns have been developed (dakos et al., 2010). In general, however, these ‘classical’ indicators show only irregular monotonic behavior and it is difficult to determine how close the system is to transition and when to give an alarm. Ideally, one likes to have the availability of indicators which give a sharp peak just before the transition.

Indicators based on complex interaction networks were shown to have this desired ‘peaky’ property when applied to a highly conceptual ecological model, the local positive feedback model (Tirabassi et al., 2014). Although the network based indicators have a higher quality factor, for this model also the classical indicators perform well regarding the desertification transition. A more challenging test of the capabilities of network based indicators is the scale-dependent feedback model suggested in Rietkerk et al. (2002). For this model, two classical indicators (lag-1 autocorrelation and Moran’s coefficient, see Sect. 2.2) show unexpected trends when approaching the critical transition (Dakos et al., 2011).

As was indicated in Dijkstra (2011), the structure of the multiple equilibria in a scale-dependent feedback model is complicated because of the appearance of a multitude of saddle-node bifurcations. Near the transition to a desert state, many other unstable steady states influence the spatio-temporal behavior of the vegetation field. This suggests that the self-organization mechanisms in such a model increases the complexity of the spatial and temporal correlations of the vegetation signal, which decreases the performance of the classical indicators. It is therefore interesting to investigate how network based indicators will perform in such a scale-dependent feedback model.

In the present study, the land-atmosphere model as presented in Konings et al. (2011) is used to test the performance of network based indicators regarding the desertification transition. This model couples land surface processes (Rietkerk et al., 2002) and the dynamics of the atmosphere boundary layer (Konings and Katul, 2010). It captures two important positive feedback mechanisms, the small-
scale biomass-infiltration positive feedback (Rietkerk et al., 2002) and the large-scale precipitation-transpiration feedback (Entekhabi et al., 1992; Dekker et al., 2007). On small scales, increasing biomass is able to promote the water infiltration rate, which will provide more soil water and in turn maintain more biomass. At large scales, increased precipitation leads to more biomass, which can increase transpiration rate and recharge water vapor in the atmosphere. Consequently more rainfall events can occur and increase the amount of precipitation. In addition to these feedbacks, also the seasonal variability of rainfall, which is shown to be important in arid and semi-arid regions (Baudena and Provenzale, 2008; Good and Caylor, 2011; Siteur et al., 2014a), is represented in the model.

Output from a large number of simulations with this model are used to reconstruct interaction networks from which early warning indicators of transitions are derived. The performance of these indicators is compared with those of classical indicators with the aim to understand the behavior of these indicators near the desertification transition. In Section 2 the essential features of the land-atmosphere model and the complex network methodology are described. Results of the simulations of the land-atmosphere model are presented in Section 3.1 and the performance of the classical and network based early warning indicators is presented in Section 3.2. A summary and discussion of the results is given in Section 4.

2 Model and methodology

2.1 The land-atmosphere model

The land-atmosphere model (Konings et al., 2011) couples a one-column atmospheric boundary layer (ABL) model (Konings and Katul, 2010) with a scale dependent feedback vegetation model (Rietkerk et al., 2002). The ABL model is seasonally forced to capture the African monsoon variability (Konings et al., 2011). The vegetation model considers the interactions among surface water, biomass dynamics and soil moisture (Rietkerk et al., 2002). The surface energy balance contains the turbulent momentum and moisture exchange between the land and atmosphere (Konings et al., 2011). In this study, state-dependent noise is included for biomass, surface water and soil moisture to represent unresolved processes (Dakos et al., 2011; Tirabassi et al., 2014); the detailed equations of the model are presented in the Appendix.

The fundamental characteristic of the land-atmosphere coupling is the water and energy exchange between the land surface and the ABL. The vegetation model simulates the biomass dynamics and determines the sensible and latent heat fluxes. The sensible heat flux \((H)\) changes the boundary layer height \((h)\) while the latent heat flux \((LE)\) affects the specific humidity \((q)\) of the atmosphere. Convective rainfall occurs when \(h\) crosses the level of free convection (LFC) and the lifting condensation level (LCL). The LFC is the altitude where the lifted parcels become buoyant, while the LCL is the height where the condensation starts. When rainfall happens, the amount of rainfall is determined...
by the total moisture content in the atmosphere and a rainfall efficiency ($\eta$). The parameter $\eta$ will be the main control parameter in the model and controls (together with other processes as transpiration, etc.) the total amount of annual precipitation.

Simulations with the model used a time step of 150 seconds and were at least 20 years and aimed to determine a statistical equilibrium state. As a criterion for reaching the equilibrium, we required that the maximum (over the whole grid) relative difference of the annual mean values of the biomass field between two neighbouring years was less than 0.5%.

The land-atmosphere model accounts for the annual cycle of solar radiation. Moreover, the observed climate forcing data (slope $\gamma$ and intercept $\phi$ of the free atmosphere for specific humidity $q$ and potential temperature $\theta$, see Appendix) contains seasonal atmospheric variability. To remove strong seasonal correlations due to forcing in the biomass time series $\hat{B}^n_i$, where $i$ refers to a location in space and $n$ to the time index, the average over $M$ years is removed for each day of the year. More specifically, for daily data with $n(j,k) = 365 \cdot (j - 1) + k$ (leap years ignored), the detrended time series $B^n_i$ is determined from

$$B^n_{i,j,k} = \hat{B}^{n,j,k}_i - \frac{1}{M} \sum_{j=1}^{M} \hat{B}^{n,j,k}_i.$$  \hspace{1cm} (1)

The zero-lag correlation coefficient between the $B^n_i$ and $\hat{B}^n_i$ is less than 0.2 in all randomly selected values of $i$, implying that the annual cycle is successfully removed from each time series. Note that the detrended biomass $B^n_i$ can have negative values as it is an anomaly with respect to the seasonal cycle. All biomass time series referred to below in this paper are seasonally detrended. Mention here the value of $M$ used.

### 2.2 Early warning indicators

One of the most commonly used indicators in the temporal approach is the lag-m autocorrelation function $R_i(m)$ at location $i$ given by

$$R_i(m) = \frac{\sum_{n=1}^{N-m} (B^n_i - \bar{B}_i)(B^{n+m}_i - \bar{B}_i)}{\sum_{n=1}^{N} (B^n_i - \bar{B}_i)^2},$$  \hspace{1cm} (2)

where $N = 365M$ is the total length of the time series and $\bar{B}_i$ is the mean of the time series. Critical slowdown is associated with an increase in the lag-1 autocorrelation $R_i(1)$.

To determine changes in spatial correlation of the biomass often Moran’s coefficient is used. As shown in the Appendix, the total number of locations in the vegetation model $K = 75 \times 75$; Moran’s coefficient at time $n$ is then given by

$$I^n = \frac{K}{\sum_{ij} g_{ij}} \frac{\sum_{ij} g_{ij} (B^n_i - \bar{B}^n)(B^n_j - \bar{B}^n)}{\sum_i (B^n_i - \bar{B}^n)^2},$$  \hspace{1cm} (3)

where $g_{ij} = 1$ if node $i$ and $j$ ($i,j \in [1,75 \times 75]$) are neighbours and $g_{ij} = 0$ otherwise. Furthermore,
**B**\(^n\) is the spatial averaged biomass \(B\) at time index \(n\) and the sums. Here we only use the spatial distribution of the biomass at the last time step of the simulation (i.e., \(n = N\)).

The new element in this paper is to consider early warning indicators based on complex networks\(^{11}\) Caldarelli (2007) which are composed of nodes and links (or edges). In this study, the nodes are the \(K = 75 \times 75\) grid cells of the vegetation model. To determine the links between two nodes, \(i\) and \(j\) we calculate the lag-0 Pearson cross correlation coefficients \(C_{ij}\) of the biomass time series at these nodes. Only the last 5-year daily biomass values are used for the calculation of the \(C_{ij}\). The nodes \(i\) and \(j\) are considered to be linked if the correlation \(|C_{ij}|\) is higher than a certain threshold value \(\tau > 0\). This threshold is determined by a significance analysis and for all the results below, \(\tau = 0.7\) guarantees significant correlations with a \(p\)-value smaller than 0.05.

The network is next represented as a graph having \(K=75 \times 75\) nodes where the links are described by an adjacency matrix \(A\). This is a \(K\times K\) symmetric matrix where the element \(A_{ij}\) is given by

\[
A_{ij} = \mathcal{H}(|C_{ij}| - \tau). \tag{4}
\]

The quantity \(\mathcal{H}\) is the Heaviside step function. Here \(A_{ij}=1\) (=0) indicates that nodes \(i\) and \(j\) are linked (not linked). Figure 1 provides an example of small network where the circles represent the (12) nodes and the red solid curves represent the links between the nodes.

By the network reconstruction, the analysis of spatio-temporal correlations in the biomass field is transformed into the analysis of topological properties of the graph (such as in Fig. 1) of the network. In this study, we focus on three topological properties: degree, assortativity and clustering.

The degree, denoted by \(d_i\) \((i \in [1,K])\), is the number of nodes that are linked with the specific node \(i\), as:

\[
d_i = \sum_{j=1}^{K} A_{ij}. \tag{5}
\]

For instance, in Fig 1 the degree of node \(i\) is 3. Note that the self correlation is ignored, thus the value of \(d_i\) varies from 0 to \(K-1\). The maximum value occurs when all nodes are significantly correlated.

The assortativity \((a_i)\) is the average degree of the neighbours of node \(i\), and given by

\[
a_i = \frac{1}{d_i^2} \sum_{j=1}^{K} A_{ij} d_j. \tag{6}
\]

In Fig 1, node \(i\) has three neighbours, the degree of each neighbour is 2 and hence the assortativity of node \(i\) is 2. The assortativity measures the second stage relations of the specific node in the network and values of \(a_i\) vary between 0 and \(K-1\).

The clustering coefficient \((c_i)\) of node \(i\) is the ratio of the number of links among the neighbours of node \(i\) to the number of possible links among its neighbours. The formula for \(c_i\) is:

\[
c_i = \frac{1}{d_i(d_i - 1)} \sum_{j=1}^{K} \sum_{l=1}^{K} A_{ij} A_{jl} A_{li}. \tag{7}
\]
For example in Fig 1, node $i$ has three neighbours. Two of its neighbours are linked but there are three possible links among these neighbours. Thus the clustering coefficient is $1/3 = 0.33$. Values of $c_i$ vary between 0 and 1 and the maximum value occurs when all neighbours of node $i$ are linked.

3 Results

Before any early warning indicator can be applied, first the different equilibrium states of the model and how simulated precipitation and biomass equilibrium fields change with $\eta$ have to be determined; this is presented in Section 3.1. Subsequently, the classical and network based indicators are applied to the simulated biomass time series in Section 3.2 and we next investigate their capabilities to serve as early warning signals of transitions between equilibria in the model (Section 3.3).

3.1 Equilibria in the land-atmosphere model

In the land-atmosphere model, the frequency and intensity of rainfall is determined by the water and energy transported from the land surface processes. As mentioned above, we use the rainfall efficiency $\eta$ as the measure of the dryness of the climate (Konings et al., 2011). For values of $\eta$ in the range from 0.7 to 1.0, branches of equilibrium solutions of the model were computed. By taking different initial conditions for similar values of $\eta$, different multiple equilibria were found. For instance, in the case of $\eta=0.84$, a desert equilibrium is found from a high biomass initial condition. However, an equilibrium state with vegetation cover can be reached from the equilibrium state obtained with $\eta=0.85$. As our main aim is to determine the performance of the early warning indicators near the desertification transition, it is not necessary to reveal all branches of equilibria in the model.

In Fig. 2, part of the bifurcation diagram of the model is plotted, showing the relation between rainfall efficiency $\eta$ and the mean daily rainfall $P$ and the equilibrium mean biomass $B$ of the equilibria. The values of $P$ and $B$ are both spatially and temporally averaged using the data of the last five years of each model simulation. The dots in Fig. 2 indicate the actual values of $\eta$ used and branches of equilibria are labelled L1-L7. Along each branch, $B$ decreases with $\eta$ and branches overlap for certain intervals of $\eta$. The desertification transition appears near $\eta=0.79$, at the left end of branch L2, from where the equilibrium biomass shifts considerably from approximately $2 \text{ g m}^{-2}$ to zero.

A different view on the properties of the solutions on the branches is obtained from Fig. 2B where $P$ is plotted versus $\eta$. The positive vegetation-precipitation feedback leads to a high correlation between $B$ and $P$. However, the $P$ does not drop to zero at branch L1 as soil evaporation exists and maintains a weak precipitation feedback. The correlation between $P$ and $B$ along the branches can also be clearly seen in the $P$-$B$ diagram (Fig. 2C). By comparing this to the same diagram without land-atmosphere coupling (Dakos et al., 2011), we deduce that the ‘gaps’ in the $P$-$B$ relation are
caused by the vegetation-precipitation feedback. This suggests that abrupt shifts of the hydrological processes (i.e., precipitation and evapotranspiration) might be hidden in the smooth curve found between mean annual precipitation and maximum woody cover in Sankaran et al. (2005).

The only overlap of branches in Fig. 2C is that of the branches L5 and L7 where the different solutions are associated with slightly different rainfall rates (Fig. 2B). However, the amount of transpiration is almost the same. This implies that more water vapor is stored in the atmosphere in the lower $\eta$ case (branch L5) as less precipitation is generated, but the water vapor recharge from transpiration is almost the same as the higher $\eta$ case (branch L7). Such water vapor accumulation process lasts until an extra precipitation occurs, meaning that with the same $P$ and a lower $\eta$ in L5 has higher rainfall frequency and yields higher $B$ than higher $\eta$ in L7. The results agree with other findings about the effect of rainfall frequency on biomass dynamics (Baudena and Provenzale, 2008; Siteur et al., 2014a). Moreover, the range of $P$ ($0.6 < P < 1.0 \text{ mm d}^{-1}$) where patterned biomass exists in Fig. 2C is narrower than in the vegetation model without land-atmosphere coupling ($0.3 < P < 1.3 \text{ mm d}^{-1}$), which coincides with the findings from Dijkstra (2011). This paragraph is still difficult to understand. Stefan/Bart, can you clean it up?

Typical vegetation patterns on each branch are shown in Fig. 3 and most overlap between branches occurs (between L2 and L4) when vegetation patterns are spots. For $\eta$ in the interval $[0.85 - 0.9]$, the environment can sustain numerous equilibria with a wide range in spot numbers. Along a branch, the spot number remains constant but different branches are associated with different spot numbers. Qualitatively similar behavior was found by (Dijkstra, 2011) in another land-atmosphere coupled model (Dekker et al., 2007). Siteur et al. (2014b) revealed that vegetation can adjust to the environment by changing biomass of patches or by shifting wavelength. The change of wavelength is associated with a jump between the branches. Only spots at the border of the domain survive along branch L2, which is different to the spot patterns on other branches. This is consistent with the results in Dijkstra (2011), where also patterns with only border spots can be sustained under low rainfall.

3.2 Early warning indicators

Figure 4 shows the two classical indicators, the lag-1 autocorrelation and Moran’s coefficient versus $P$ (using the values in Fig. 2B) and the behavior of the two indicators is similar. A sharp increase with decreasing $\eta$ occurs along branch L6, implying that the indicators are sensitive to the shift of biomass from a homogeneous distribution to a labyrinth patterns (Fig. 2 and 3). The indicators drop sharply from L6 to L5 and then gradually increase until L2. When the state is approaching the desertification transition along L2, the value of indicators drops considerably. The trend coincides with the results from Dakos et al. (2011) where both the classic indicators do not smoothly increase with the decrease in rainfall and a sharp drop occur before the upcoming desertification. Even though the sharp decrease of the indicators is a clear early warning signal of the upcoming critical transition,
their behavior is quite irregular and can easily lead to a false alarm.

We now turn to the network based indicators and show in Fig. 5a the distribution of the degree of a network determined for a value of $\eta$ along the different branches (Fig. 3). Two values of $\eta$ (0.79 and 0.85) are chosen along the branch L2 to illustrate the large change in the degree distribution before the desertification transition. All distributions are bimodal with the first peak fixed at zero while the second peak increases from approximately 500 (L6) to 4000 (L3) and then decreases along the branch L2. Similar behavior occurs for the assortativity of the networks (Fig. 5b) and the clustering coefficient (Fig. 5c). As in Tirabassi et al. (2014), the network based indicators will be determined from the properties of the distribution of each network quantity.

Figure 6 shows these network based indicators as a function of $P$. Degree, assortativity and clustering are listed in columns. The properties of the distributions (mean, standard deviation, skewness and kurtosis) are plotted in rows. All moments are determined by the shift of the bimodal distribution (Fig. 5a). Both the mean and variance of the degree distribution how a similar variation with $P$ as the classical indicators (Fig. 2). However, the relative drop of the network based indicators near the desertification transition (e.g., from 2000 to 200 for the mean degree) is much larger than that for the classical indicators. The skewness (Fig. 6) is influenced by the areas of the two peaks in the degree distribution (Fig. 5a). With decreasing $P$, the skewness degree drops until -1 and sharply increases before the desertification transition. Although the skewness degree varies over a small range, the sign change can be a useful early warning indication for the desertification transition. Note that such sign change only occurs only along branch L2. The kurtosis of the degree distribution also presents a useful indicator as it is small and near constant at high $P$ end of branch L2 and then increases sharply with decreasing $P$.

In the middle column of Fig. 6 the properties of the distribution the network assortativity is shown. Bimodality is also found in the assortativity (Fig. 5b) where the movement of the second peak is the same as that of the degree distribution. The behavior of the mean, standard deviation and skewness of the assortativity distribution are similar to that of the degree. The kurtosis behaves different in that it decreases with decreasing $P$ and is not constant at the high $P$ end of branch L2. It is interesting that the behavior of the skewness of the assortativity is similar to that found in the local positive feedback model (Tirabassi et al., 2014). This suggests that this indicator might be a more broadly applicable signal for transitions in a wide range of ecological models.

Finally, in the right column of Fig. 6, the properties of the distributions of clustering coefficient of the networks are shown. The behavior of the mean, skewness and kurtosis of the clustering coefficient is very similar to that of the assortativity; the standard deviation, however, increases with decreasing $P$. The position of the second peak in the clustering distribution moves only slightly with $P$ (Fig. 5c), which leads to relatively small changes in mean and standard deviation (Fig. 6). However, the kurtosis of the distribution changes dramatically and leads to a sharp peak when the state shifts from L3 to L2 (Fig. 6).
3.3 Quality measures of the indicators

At first sight, both classical and network indicators could be used as early warning indicators of the desertification transition. However, the sensitivities of these indicators to changes in $P$ are quite different. It is hard to distinguish whether sudden changes in an indicators contains a ‘real’ early warning signal or is just due to the strong variation of this quantity. Hence it is important to determine and evaluate measures of quality of the indicators. We propose three measures to assess the quality of the indicators. Each of them can be written in the form

$$D = \frac{|\Psi_1 - \Psi_2|}{|\Psi_1| + |\Psi_2|},$$

(8)

where $\Psi_1$ and $\Psi_2$ are the two specific quantities that are compared. A high (low) value of $D$ implies a large (small) difference between $\Psi_1$ and $\Psi_2$ and vice versa.

The first measure, denoted by $D_m$, focuses on the sudden change of an indicators along the L2 branch (cf. Fig. 4). It evaluates the magnitude of the difference between the mean of the specific indicator before and after the sudden shift in L2. Points with $\eta \leq 0.82$ are classified as the states after the sudden shift while points with $\eta \geq 0.851$ are classified as the states before the sudden shift. For each indicator, the mean values of the two point groups are set as $\Psi_1$ and $\Psi_2$ in Eq. 8 to calculate $D_m$. Indicators with a large shift along L2 will have higher values of $D_m$. ”Note that the mean value of the skewness may be negative, which is not accounted in this assessment.” Vincent: I modified (8) to take this into account; values should be corrected in Table 2.

The second measure ($D_r$) considers the difference of variations before and after the sudden shift in L2. The two point groups are classified as for the $D_m$ measure and because only a few points are available in each group, the the difference between the maximum and the minimum value is used as the approximation of the variance in the Eq 8. High values of $D_r$ indicate that the specific indicator has a significant variation along the branch L2 and hence is less suited as an early warning signal.

Table 2 presents the assessment of all indicators by the three measures: a good indicator ideally has a high value of $D_m$ and low values of $D_r$. The classical indicators have typically much lower values of $D_m$ than the network indicators. Highest values of $D_m$ are found for the mean degree, the mean assortativity and the kurtosis of the clustering distribution. Highest quality indicators are the standard deviation of the degree and of the assortativity. In general, early warning signals of network indicators have a higher quality than the classical indicators. Vincent: maybe adapt this paragraph when skewness values become available.
4 Summary and Discussion

In this study, we evaluated the performance of early warning indicators for the desertification transition in a coupled land-atmosphere model. In contrast to other ecological models (Dakos et al., 2011; Tirabassi et al., 2014), multiple overlapping branches of equilibria were found in this model. Three criteria were applied to assess the quality of early warning indicators and the results showed that the network based indicators have a relatively high quality compared to the classical ones.

The land-atmosphere coupled model (Konings et al., 2011) captures two feedback mechanisms. The local infiltration positive feedback results in regular vegetation patterns, which changes with the total amount of precipitation. The vegetation-precipitation feedback leads to the discrete $P$-$B$ lines in Figure 2C. Multiple stable branches (L2, L3 and L4) are found after vegetation patterns shift from labyrinth to patches and transitions are caused by the change of number or position of patches (Dijkstra, 2011; Siteur et al., 2014b). The catastrophic shift to desertification (from L2 to L1 in Fig. 2) is associated with the disappearance of the boundary patches.

This behaviour of the model equilibria explains why most of indicators increase from L5 to L4, then keep a near constant value down to L2 and drop sharply before the desertification Dakos et al. (2011). The indicators do detect potential critical transitions as they change substantially when multiple stable states exist (from L5 to L2). As was found in Dijkstra (2011), all branches of equilibria already exist with the infiltration feedback. The vegetation-precipitation feedback only shifts the branches and hence does not appear to be important for the existence of the desertification transition, but determines the value of $P$ for which this occurs.

The behavior of the classical indicators is similar to that of most network based indicators. However the network based indicators are more sensitive to upcoming critical transitions and the signals can be easier distinguished from local variations. This does not mean that classical indicators can be abandoned as they provide early warning signals at an very early stage of transition (Scheffer et al., 2009; Dakos et al., 2011). However, the network based indicators provide more peaky signals when the critical transition is approached (Tirabassi et al., 2014) and hence form a useful addition to the classical indicators.

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Bibliography

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Table 1: Values of parameters in the land-atmosphere coupled model
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<th>Variable</th>
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<th>$D_r$</th>
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Table 2: Evaluation of the quality of the early warning indicators by the two different measures $D_m$ and $D_r$.

**Figures**

Fig. 1: Diagram to illustrate a complex network and its properties (from Tirabassi et al. (2014)). Circles indicate the grid cells of $B$ and form the nodes of the network. Solid lines indicate the links between the nodes. Node $i$ has degree $d_i=3$, clustering coefficient $c_i=0.33$ and assortativity $a_i=2$. 
Fig. 2: The relation between the rainfall efficiency $\eta$, the mean biomass $B$ (panel A) and the mean precipitation $P$ (panel B), with a $P$-$B$ diagram in panel C. Solid lines indicate equilibria of the model and the dots indicate the actual values found in the model simulations.

Fig. 3: Equilibrium biomass patterns at different branches shown in the Figure 2. The plots are based on the biomass at the last time step of the simulation. The specific rainfall efficiency values $\eta$ are: L2:0.79; L3:0.857; L4:0.87; L5:0.92; L6:0.962; L7:0.98.
Fig. 4: The behavior of the classical indicators versus $P$ with in the left panel the lag-1 autocorrelation and in the right panel Moran’s coefficient. Moran’s coefficient is based on the spatial distribution of biomass at the last time step of the simulation. Dashed lines reveal the regions of different branches shown in Fig. 2.

Fig. 5: The distribution of the network properties (a) degree, (b) assortativity and (c) clustering coefficient along the different branches (distinguished by the colors). The solid and dashed curves represent the two samples from L2. The specific $\eta$ of the samples are: L2:0.79 (dashed) and 0.85 (solid); L3:0.869; L4:0.87; L5:0.883; L6:0.968.
Fig. 6: Network based indicators as a function of mean annual rainfall $P$. Three network variables are listed in columns and different statistic indicators are listed in rows. The diagrams are divided by red dashed lines into six regions for different branches.
Appendix A

Model description

A1 Atmospheric boundary layer model

The potential temperature ($\theta$) and the specific humidity ($q$) varies with the height of the ABL. For simplicity the model assumes that the energy and water vapor are well mixed in the ABL. Consequently $\theta$ and $q$ are constant in the ABL. On the top of ABL, both $\theta$ and $q$ are assumed to have a linear relation with the height above the surface $z$, as:

$$\theta(z) = \gamma_{\theta} z + \phi_{\theta}$$

$$q(z) = \gamma_{q} z + \phi_{q}$$

where $\gamma$ and $\phi$ are slope and intercept, respectively.

The change of the $h$ in time $t$ is as a function of latent heat flux,

$$\frac{dh}{dt} = \frac{(1 + 2A)(\theta'\omega')_s}{\gamma_{\theta} h}$$

where $(\theta'\omega')_s$ is the sensible heat flux from the surface; $A$ is the ratio of the sensible heat flux at the top of the ABL to the surface sensible heat flux, which is called Tennekes parameter and assumed as constant (0.2).

When the ABL grows, the heat and humidity fluxes in the top of the ABL is proportional to the difference between the value on the top of the ABL and the value below the fluxes. The temperature and humidity of the ABL can be estimated by the conservation equations:

$$h \frac{d\theta}{dt} = (\theta'\omega')_s + (\gamma_{\theta} h + \phi_{\theta} - \theta) \frac{dh}{dt}$$

$$h \frac{dq}{dt} = (q'\omega')_s + (\gamma_{q} h + \phi_{q} - q) \frac{dh}{dt}$$

where $(q'\omega')_s$ is the sensible heat flux at the surface. The $(\theta'\omega')_s$ and $(q'\omega')_s$, which are calculated in the vegetation model, are described in the Section A2.

The precipitation occurs only when the $h$ crosses the height of the LFC and LCL. Another condition, $z/L \geq 5$, is included in the model of Konings et al. (2011) to make sure that the air parcels are able to rise from the LFC to the LCL. Here $L$ is the Obukhov length:

$$L = \frac{u^3_{*} \theta}{\kappa_v g (\theta'\omega')_s}$$

where $z = h/2$ is the center of the ABL; $\kappa_v$ is von Karman’s constant; $g$ is the acceleration due to gravity; $u_*$ is the friction velocity.
The amount of rainfall is proportional to the total water vapor in the atmosphere column. The moisture over the height of the free atmosphere is also taken into account. Following Konings et al. (2011) to prevent the uncertainties from the free atmosphere, the model accounts for the water vapor in the atmosphere column with double height of the ABL, as:

\[ P = \eta_{\text{max}} \eta \int_{0}^{2h} q \, dz \quad (A7) \]

where \( P \) is the amount of rainfall and the duration is set at two hours; \( \eta_{\text{max}} \) (0.33) is the maximum rate that the water vapor can transform into rainfall; \( \eta \in [0,1] \), called rainfall efficiency, is a free parameter to account for all factors that influences the rainfall process.

### A2 Vegetation dynamics model

The vegetation model (Rietkerk et al., 2002) integrates the surface energy balance in the vegetation dynamics to simulate the water and heat feedback to the atmosphere (Konings et al., 2011). In this study, we consider a lattice with \( 75 \times 75 \) grid cells. The dynamics of surface water content \((O)\), soil water content \((W)\) and biomass \((B)\) are simulated in each cell with stochastic process (Dakos et al., 2011). The horizontal exchange of water and biomass are estimated at the boundary of neighbouring cells. The vertical fluxes of water and energy from the land to the atmosphere (e.g., transpiration, sensible heat flux, etc) are averaged values of all grid cells. Precipitation \((P)\) is the only source that can recharge the water in the vegetation model. The \( O \) obtains water from \( P \) and re-distribute it spatially or vertically. The dynamical equation of \( O \) is written as:

\[ \frac{\partial O}{\partial t} = P - \alpha_0 \frac{B + k_2 W_0}{B + k_2} O + D_O \nabla O + \sigma_O O \xi^O(t) \quad (A8) \]

\( O \) can lose water due to infiltration (the second term in Eq A8). The infiltration rate is determined by current \( O \) and \( B \) (Rietkerk et al., 2002). \( \alpha_0 \) is the maximum infiltration rate; \( k_2 \) is the saturation constant of infiltration; \( W_0 \) is the relative infiltration fraction of bare soil. \( D_O \nabla O \) is the diffusion of the surface water \( O \) with diffusivity \( D_O \). \( \sigma_O O \xi^O(t) \) is the noise of the \( O \). The noise is a proportional to \( O \). \( \xi^O(t) \) is Guassian white noise with standard deviation \( \sigma_O = 0.01 \).

The soil water content \( W \) is recharged by infiltration of \( O \) and lost by evapotranspiration and deep soil drainage. The governing equation is:

\[ \frac{\partial W}{\partial t} = \alpha_0 \frac{B + k_2 W_0}{B + k_2} O - E_t - E_s - r_w W + D_W \nabla W + \sigma_W W \xi^W(t) \quad (A9) \]

The first term is the infiltration rate of \( O \), which is the same as Eq A8. \( E_t \) and \( E_s \) are vegetation transpiration and bare soil evaporation, respectively. \( r_w W \) is the deep soil drainage, which is proportional to \( W \) with a constant rate \( r_w \). The diffusion and noise term are similar to Eq A8.

The \( E_t \) and \( E_s \) are linearly related with latent heat fluxes of vegetation and bare soil respectively, as:

\[ E_s = \frac{LE_s}{\lambda \rho_{\text{H}_2\text{O}}} \quad (A10) \]
\[ E_t = \frac{LE_t}{\rho \lambda_{\text{H}_2\text{O}}} \]  

(A11)

where \( \rho \lambda_{\text{H}_2\text{O}} \) is the water density; \( LE_t \) and \( LE_s \) are latent heat fluxes of vegetation and bare soil respectively, which are estimated by the Penman-Monteith equation, as:

\[ LE = \frac{\Delta (R_n - G) + \rho c_p VPD r_{\text{a}} \Delta + \gamma (1 + r_s r_{\text{a}})}{\Delta + \gamma (1 + \frac{r_s}{r_{\text{a}}})} \]  

(A12)

\( LE \) is the latent heat flux of the bare soil or vegetation, which is determined the parameterization of the surface resistance \( r_s \). \( R_n \) is the net radiation; \( G \) is the soil heat flux; \( \rho \) is the air density; \( c_p \) is the specific heat capacity of the air; \( VPD \) is the vapor pressure deficit; \( \Delta \) is the slope of the saturated vapor pressure to temperature; \( \gamma \) is the psychrometric constant, which is a function of the surface pressure and the latent heat of evaporation \( \lambda \), as \( \gamma = c_p P_s / (0.622 \lambda) \). \( r_a \) is the aerodynamic resistance; \( r_s \) is the surface resistance. When calculating vegetation latent heat flux \( LE_t \), the model use the stomatal resistance \( r_{E_t} \) as \( r_s \). When \( r_s \) represents the bare soil resistance \( r_{E_s} \), the latent heat flux of the soil \( LE_s \) will be calculated.

The stomatal resistance \( r_{E_t} \) is a function of \( W \), VPD and leaf area index (LAI). The LAI is positive related with the biomass \( B \). For simplicity Konings et al. (2011) assume a linear function as \( \text{LAI} = \alpha_1 B \), which holds due to the low values in \( B \) in this semi-arid region. \( \alpha_1 \) represent the constant ratio of LAI to \( B \). The formula of \( r_{E_t} \) is:

\[ \frac{1}{r_{E_t}} = \frac{1}{r_{E_{\min}}} \frac{W}{W + k_1} (1 - m \log(VPD)) \alpha_1 B \]  

(A13)

Where \( r_{E_{\min}} \) is the minimum stomatal resistance per unit LAI; \( k_1 \) is the saturated water stress; \( m \) is a factor used to represent the increase rate of resistance with decreased VPD.

The soil resistance \( r_{E_s} \) is calculated as:

\[ \frac{1}{r_{E_s}} = \frac{1}{r_{E_{\min}}'} \frac{W}{W + k_3} \left( 1 - \frac{B}{B + k_3} \right) \]  

(A14)

Where \( r_{E_{\min}}' \) is the minimum soil resistance; \( k_3 \) is the constant used in the function to estimate the effect of biomass shade to soil evaporation.

The dynamics of biomass is determined by carbon assimilation rate and respiration. Carbon assimilation positively relates to the amount of biomass \( B \) and CO\(_2\) gradient between inside and outside of the stomata, while the respiration rate is determined by \( B \) and the air temperature \( T_a \). The formula is given as:

\[ \frac{\partial B}{\partial t} = (g_{\text{CO}_2} c C_1 \alpha_1 B - Re(T_a) B) \frac{1}{\tau(W)} + D_B \nabla B + \sigma_B B \xi^B(t) \]  

(A15)

Where \( g_{\text{CO}_2} \) is the stomatal conductance of CO\(_2\); \( c \) is the CO\(_2\) gradient between the atmosphere and the internal space of stomata; \( C_1 \) is the conversion rate between carbon gain and biomass growth. \( Re(T_a) \) is the respiration rate with specific air temperature \( T_a \). \( \tau(W) \) indicates the drought adaption
of the vegetation. The diffusion and noise term are similar to Eq A8.

The stomatal conductance $g_{\text{CO}_2}$ is determined by the opening of the stomata, which has a linear positive relation with $E_t$, as:

$$g_{\text{CO}_2} = \nu \frac{E_t}{q - q^*}$$  \hspace{1cm} (A16)

Where $\nu$ is the ratio of CO$_2$ stomatal conductance to H$_2$O stomatal conductance; $q$ is the surface specific humidity; $q^*$ is the saturated specific humidity. The respiration rate is governed by a Q$_{10}$ function as:

$$Re(T_a) = R_b Q_{10}^{\frac{T_a-10}{10}}$$  \hspace{1cm} (A17)

Where $R_b$ is the referred respiration rate at 10°C. The $\tau(W)$ is given as:

$$\tau(W) = \frac{1}{4} W^2 + f k_4$$  \hspace{1cm} (A18)

Where $k_4$ is a constant related to soil water; $f$ is the metabolic rate without water. Note that the time step of the biomass dynamics is 1 day, which is different with the time interval (2.5 min) of the ABL and water simulations.

The surface energy budget is composed by net radiation $R_n$, sensible heat flux $H$, latent heat flux $LE$ and soil heat flux $G$. The net radiation is calculated by:

$$R_n = (1 - \alpha) R_s + \epsilon_s \sigma (\epsilon_a T_a^4 - T_s^4)$$  \hspace{1cm} (A19)

Where $\alpha$ is the surface albedo, which is linearly interpolated between $\alpha = 0.25$ when $B = 0$ g m$^{-1}$ and $\alpha = 0.15$ when $B = 25$ g m$^{-1}$. $\sigma$ is the Stefan-Boltzmann constant; $\epsilon_s$ and $\epsilon_a$ are emissivity of the surface and atmosphere respectively. $R_s$ is the incoming shortwave radiation. It is a function of number of day DOY, hour angle $h_a$ and the latitude $\phi$. It is given by:

$$R_s = R_0 \frac{\cos \beta}{r^2}$$  \hspace{1cm} (A20)

Where $R_0$ is the solar constant; $r$ is a factor to correct the distance between the earth and the sun; $\beta$ is the solar zenith angle. The $r$ is determined by the DOY as:

$$r = 1.0 + 0.017 \cos \frac{2\pi}{365} (186 - \text{DOY})$$  \hspace{1cm} (A21)

The $\beta$ is affected by the hour angle and the latitude $\phi$, as:

$$\cos \beta = \cos \phi \cos h_a \cos \delta + \sin \phi \sin \delta$$  \hspace{1cm} (A22)

Where $\delta$ is the solar declension.

The sensible heat flux $H$ is a function of surface resistance and the temperature gradient between the surface and the atmosphere:

$$H = \frac{\rho c_p}{r_a} (T_a - T_s)$$  \hspace{1cm} (A23)
Here \( r_s = h_{s\alpha}/(z_o \kappa_w u_s) \). \( h_{s\alpha} \) and \( z_o \) are the height of the surface layer and the surface roughness respectively. The \( z_o \) is determined by the canopy height \( h_c \) as \( z_o = 0.1 h_c \) and \( h_c = 0.05/(3B) \).

The land surface energy balance equation is:

\[
R_n - \lambda \rho E_t - \lambda \rho E_s - G - H = 0
\]  
(A24)

Where \( G = 0.15 R_n \) is the soil heat flux. There are three unknowns \( (R_n, H \) and \( T_s) \) in Equation A19, A23 and A24, from where the energy balance of the surface can be estimated. The simulated \( H \) and \( LE \) are used to determine the surface sensible and latent heat fluxes in the atmosphere model as:

\[
\overline{(\theta' \omega')} = \frac{H}{\rho c_p}
\]
(A25)

\[
\overline{(q' \omega')} = \frac{LE}{\rho c_p}
\]
(A26)

All parameters are listed in Table 1.